4E4161

Roll No.

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B. Tech. IV Sem. (Main/Back) Exam., June/July-2014 Computer Science and Engineering 4CS2A Discrete Mathematical Structures Common with IT

Time: 3 Hours

Maximum Marks: 80

Min. Passing Marks: 24

Instructions to Candidates:-

Attempt any five questions, selecting one question from each unit. All Questions carry equal marks. Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly.

Units of quantities used/calculated must be stated clearly.

Use of following supporting material is permitted during examination.

(Mentioned in form No.205)

NIL

NIL

UNIT-I

Q.1 (a) (i) Prove, for finite sets A and B;

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

[4]

(ii) In a class of 50 students, 15 play Tennis, 20 play Cricket and 20 play Hockey, 3 play Tennis and Cricket, 6 play Cricket and Hockey, and 5 play Tennis and Hockey. 7 play no game at all. How many play Cricket, Tennis and Hockey?
[4]

[10080]

	(b)	(i) Define floor function and ceiling function with example.	[4]
		(ii) "If f and g are two bijections such that gof is defined then gof i	s also a
		bijection." Prove it.	[4]
		<u>OR</u>	
Q.1	(a)	(i) If $f: A \to B$ be one-one onto then the inverse map of f is unique. Pro	ve it.
			[4]
8		(ii) Show that set of even positive integers is a countable set.	[4]
	(b)	Sate and prove the Pigeonhole and Generalized Pigeonhole Principles.	[8]
		<u>UNIT – II</u>	
Q.2	(a)	Define the following with example:-	
		(i) Equivalence relation	[2]
		(ii) Congruence relation	[2]
		(iii) Partial order relation	[2]
		(iv) Total order relation	[2]
	(b)	Explain closure of relations. Let $A = \{1,2,3,4\}$ and let $R = \{(1,2),(2,3,4)\}$	3) (3,4),
		(2,1)} be a relation on A. Find the transitive closure of R using Wa	ırshall's
		algorithm.	[8]
		<u>OR</u>	
Q.2	(a)	Let $A = Z$, the set of integers relation R define in A by aRb as "a is cong	ruent to
*		b mod 2". Prove that R is an equivalence relation.	[8]
67	(b)	(i) Show that $(Z^+, divisibility)$ is a poset.	[4]
		(ii) Compute the number of partitions of a set with four elements.	[4]
	9		<i>2</i> 1
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<u>UNIT – III</u>

Q.3	(a)	(i) Prove pv $(q \Lambda r) \equiv (p V q) \Lambda (p V r)$.	[4]
		(ii) Write contrapositive, converse and inverse of the statement.	
		"The home team wins whenever it is raining". Also construct the truth to	able
		for each statement.	[4]
	(b)	(i) Prove that the linear search algorithm works correctly for every $n \ge 0$.	[4]
		(ii) Sort the list $X = \{64, 25, 12, 22, 11\}$ using selection sort algorithm.	[4]
		<u>OR</u>	54
Q.3	(a)	Every amount of postage of 12 cents or more can be formed using just 4-cent	and
		5-cent stamps. Prove this by using principle of complete induction.	[8]
	(b)	Prove the implication "If n is an integer not divisible by 3, then $n^2 \equiv 1 \pmod{3}$ "	,,
			[8]
		<u>UNIT – IV</u>	
Q.4	(a)	Define the following with example:-	
		(i) Complete graph,	[2]
		(ii) Bipartite graph,	[2]
		(iii) Isomorphic graph,	[2]
	0	(iv) Planar graph,	[2]
	(b)	(i) Suppose that $G = (V,E)$ be a graph with K – component, where e	ach
		component is a tree. Derive a formula in terms of V , E and K.	[4]
		(ii) Let there is a tree with n-vertices of degree 1, 2 vertices of degree	2 ,
		4 vertices of degree 3 and 3 vertices of degree 4. Obtain the value of n.	[4]
٠		<u>OR</u>	0
Q.4	(a)	Prove that a simple graph with n vertices and k components can have almost	
8		$\frac{1}{2}[(n-k)(n-k+1)] \text{ edges.}$	[8]
	(b)	Show that the complete bipartite graph $k_{3,3}$ is a non – planar graph.	[8]
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Q.5	(a)	(i)	Explain Tautology, contradiction and contingency.	[2]
		(ii)	Show that $(p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$ is a tautology.	[2]
		(iii)	Show that p $\Lambda \sim p$ is a contradiction.	[2]
		(iv)	Show that $(p \rightarrow q) \Lambda (p V q)$ is a contingency.	[2]
	(b)	the validity of the following argument:		
		If I l	ike mathematics, then I will study.	
		Eithe	er I study or I fail.	
		Ther	refore, if I fail then I do not like mathematics.	[8]
			<u>OR</u>	
Q.5	(a)	Chec	ck the validity of the following argument:	10
		Lion	s are dangerous animals.	
		Ther	re are lions.	
		Ther	refore, there are dangerous animals.	[8]
	(b)	(i)	Define the quantifiers. Explain types of quantifiers.	[4]
		(ii)	Over the universe of animals, let	
			P(x): x is a whale; $Q(x)$: x is a fish	
			R(x): x lives in water.	
			Translate the following into English	
			$\exists x (\sim R(x))$	
			$\exists x (Q(x) \Lambda \sim P(x))$	
			$\forall x (P(x) \land R(x)) \rightarrow Q(x)$	[4]